

10/14

Chapter 11 - Managing TE

Last Lecture

Managing TE

- Forwards/Futures
- Options
- Money Market (same as IRP)

This Lecture

We will review two cases: Receivables in FC and Payables in FC.

Example 1: CASE I - Receivables in FC

MSFT exports Windows to Switzerland for CHF 3M Payment due in 90 days.

$S_t = 0.60$ USD/CHF

TE(in USD) = CHF 3M * 0.60 USD/CHF = USD 1.8M

To manage TE, MSFT considers the following tools: forwards/futures, options, Money market instruments (used to replicate IRPT). MSFT also considers keeping the position open –i.e., no hedging.

Hedging Tools- Futures/Forwards/Options/Money Market Hedge/Do Nothing

Data:

Interest USD = **5%** - 5.125%

Interest CHF = 4% - **4.25%**

$F_{t,90\text{-day}} = .650$ USD/CHF - .651 USD/CHF

Put ($X_p = 0.64$ USD/CHF; $p_p = \text{USD } .059\text{-.}060$)

Call ($X_c = 0.63$ USD/CHF; $p_c = \text{USD } .019\text{-.}020$)

T = 90 days

Possible scenarios for S_{t+90} (distribution for S_{t+90} based on the ED)

<u>S_{t+90}(USD/CHF)</u>	<u>Probability</u>
0.58	.10
0.62	.10
0.65	.50
0.68	.30

1. Forward Hedge – Sell Forward CHF

Sell CHF forward at $F_{t,90\text{-day}} = .65$ USD/CHF

Amount to be received in 90 days = CHF 3M * 0.65 USD/CHF = USD 1.95M

Note: No uncertainty. MSFT will receive USD 1.95M, regardless of S_{t+90} .

2. MMH (Replication of IRP) – borrow FC, convert to DC, deposit in domestic bank

- Today, we do the following:
- (1) Borrow CHF at **4.25%**
 - (2) Convert to USD at 0.60 USD/CHF
 - (3) Deposit in US Bank at **5%**

MMH Calculations:

Amount to be borrowed = $\text{CHF}3\text{M}/(1+.0425*90/360) = \text{CHF } 2.9684\text{M}$

CHF 2.9684M * 0.60 USD/CHF = **USD 1.781M** = amt to be deposited in US Bank

Amount to be received in 90 days = **USD 1.781M** $(1+.05*90/360) = \text{USD } 1.8032\text{M}$

Note: There is no uncertainty about how many USD MSFT will receive for CHF 3M.

Compare FH vs MMH: MSFT should select the **FH**. MMH is *dominated* by FH.

3. Option Hedge -Buy CHF puts: $X_p = 0.64 \text{ USD/CHF}$, $p_p = \text{USD } .06/\text{CHF}$

Floor = **0.64 USD/CHF** * CHF 3M = USD 1.92 M - Total premium cost

Premium cost = CHF 3M * **USD .06/CHF** = USD .18M

Opportunity Cost (OC) = USD .18M * **.05** * .25 = USD .0025M

Total premium cost = Premium cost + OC = **USD .1825M**

Scenarios

S_{t+90} (USD/CHF)	Probability	Exercise?	Amount received (Net of cost, in USD)
0.58	.20	Yes	1.92M - .1825M = 1.7375M
0.62	.20	Yes	1.92M - .1825M = 1.7375M
0.65	.50	No	1.95M - .1825M = 1.7675M
0.68	.30	No	2.04M - .1825M = 1.8575M

$E[\text{Amount to be received in 90 days}] = (1.7375)*.2 + (1.7675)*.5 + (1.8575)*.3 = \text{1.7885M}$

Notes:

1. An option establishes a worst case scenario. In this case, MSFT establishes a *floor*, a minimum amount to be received: USD 1.92M (or net USD 1.7375).

2. The opportunity cost (OC) is included to make a fair comparison with FH and MMH, which require no upfront payment. (OC=Time value of money!)

Compare FH vs OH: **FH** seems to be better; but preferences matter. A risk taker may like the 30% chance of doing better with the **OH**.

4. No Hedge (Leave position open, that is, do nothing and wait 90 days)

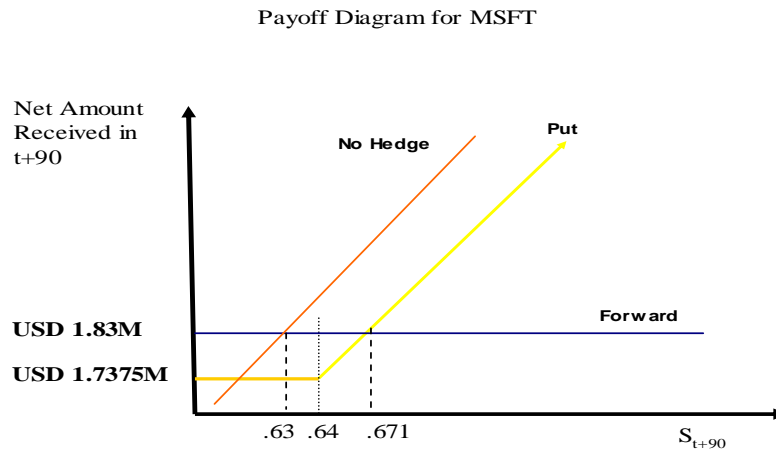
Scenarios

S_{t+90} (USD/CHF)	Probability	Amount received (Net of cost)
0.58	.10	USD 1.74M
0.62	.10	USD 1.86M
0.65	.50	USD 1.95M
0.68	.30	USD 2.04M

$E[\text{Amount to be received in 90 days}] = \text{USD } 1.947\text{M}$

Compare FH vs NH: NH seems to be better. But, preferences matter (a very conservative manager might not like the 20% chance of the NH doing worse than the FH).

Graph 11.1: General CF Diagram for all Strategies



Graph 11.1 displays the CF for all hedging strategies. In general, the preference of one alternative over another will depend on the probability distribution of S_{t+90} . If the probability of $S_{t+90} > .63$ USD/CHF (the break even S_{t+90} that makes the CF under the FH and the NH equal) is very low, then the forward hedge dominates.

Q: Where do the probabilities come from? We can estimate them using the empirical distribution (ED).

Example: CASE II - Payables in FC

MSFT has payable in GBP for GBP 10M in 180 days.

$S_t = 1.60$ USD/GBP

TE(in USD) = USD 16M

MSFT decides to manage this TE with the following tools:

Hedging Tools: Futures/Forwards/Options/Money Market Hedge/Do Nothing

Data:

Interest USD = 5%-5.25%

Interest GBP = 6%-6.5%

$F_{t,180\text{-day}} = 1.58$ USD/GBP

Put ($X_p = 1.64$ USD/GBP; $p_p = \text{USD } .05$)

Call ($X_c = 1.58$ USD/GBP; $p_c = \text{USD } .03$)

Distribution for S_{t+90}

<u>S_{t+90} (USD/GBP)</u>	<u>Probability</u>
1.55	.30

1.59	.60
1.63	.10

Which alternative is best? The hedge that delivers the least USD amount

1. FH – Buy forward GBP

Amount to be paid in 180 days = GBP 10M*1.58 USD/GBP = **USD 15.8M**

2. MMH –Borrow DC, convert to FC, deposit in foreign bank

Today, we do the following: (1) Borrow USD at 5.25
 (2) Convert to GBP at 1.60 USD/GBP
 (3) Deposit in US Bank at 6%

MMH Calculations (we go backwards):

Amount to deposit = $10M/[1+(.06*180/360)] = \text{GBP } 9.708M$

Amount to borrow = $\text{GBP } 9.708M * 1.60 \text{ USD/GBP} = \text{USD } 15.533M$

Amount to repay = $\text{USD } 15.533 * (1+.0525*180/360) = \text{USD } 15.94M$

Compare FH vs MMH: **FH is better**

3. Option Hedge –Buy GBP calls: $X_c = 1.58 \text{ USD/GBP}$, $p_c = \text{USD } .03/\text{GBP}$

Cap = $\text{GBP } 10M * 1.58 \text{ USD/GBP} = \text{USD } 15.8M$

Total premium cost = Total premium + OC = $10M * \text{USD } .03 * (1+.05*.5) = \text{USD } .31M$

Scenarios

S_{t+90} (USD/GBP)	Probability	Exercise?	Amount paid (Net of cost, in USD)
1.55	.30	No	$\text{USD } 15.5M + .31M = \text{USD } 15.81M$
1.59	.60	Yes	$\text{USD } 15.8M + .31M = \text{USD } 16.11M$
1.63	.10	Yes	$\text{USD } 15.8M + .31M = \text{USD } 16.11M$

$E[\text{Amt to be paid in 180 days}] = \text{USD } 16.02M$

Compare FH vs OH: **FH is better always.** (Preferences do not matter.)

Note: Again, the option establishes a worst case scenario. In this case, MSFT establishes a *cap*, a maximum amount to be paid: USD 15.8M (or net USD 16.11M).

4. No Hedge –leave position open; that is, do nothing and wait.

$E[\text{Amt}] = \text{GBP } 10M [1.55(.3)+1.59(.6)+1.63(.1)] = \text{USD } 15.82M$

Compare FH vs OH: **FH is better; but preferences matter.**

- **Summary of Strategies**

	Receivables in FC	Payables in FC
Forward Hedge (FH)	Sell FC at $F_{t,T}$	Buy FC at $F_{t,T}$
Money Market Hedge (MMH)	Borrow FC at i_{FC} , Convert to DC at S_t , Deposit DC at i_{DC}	Borrow DC at i_{DC} , Convert to FC at S_t , Deposit FC at i_{FC}
Option Hedge (OH)	Buy FC puts; pay p_p	Buy FC calls; pay p_c

Options hedging (with different X)

With options it is possible to play with different strike prices –different insurance coverage.

Key Intuition: The more the option is out of the money, the cheaper it is.
The higher the cost, the better the coverage.

Example: Revisit MSFT payables situation: MSFT has to pay GBP 10M in 180 days.

Notation: X_j = Strike Price (j = call; put)

p_j = Option premium (j = call; put)

$S_t = 1.60$ USD/GBP

Options available:

$X_c = 1.56$ USD/GBP, $p_c = \text{USD } .08$, T=180 days (call)

$X_c = 1.58$ USD/GBP, $p_c = \text{USD } .07$, T=180 days (call)

$X_c = 1.63$ USD/GBP, $p_c = \text{USD } .05$, T=180 days (call)

$X_c = 1.65$ USD/GBP, $p_c = \text{USD } .04$, T=180 days (call)

$X_p = 1.58$ USD/GBP, $p_p = \text{USD } .055$, T=180 days (put)

$X_p = 1.61$ USD/GBP, $p_p = \text{USD } .095$, T=180 days (put)

1. Out-of-the-Money ($S_t < X$)

Alternative 1: Call used: $X_c = 1.63$ USD/GBP, $p_c = \text{USD } .05$

Cost = Total premium = GBP 10M * USD .05/GBP = **USD 500K**

Cap = worst amount to be paid = 1.63 USD/GBP * GBP 10M = USD 16.3M

(Net cap = **USD 16.8**)

Alternative 2: Call ($X_c = 1.65$ USD/GBP, $p_c = \text{USD } .04$)

Cost = GBP 10M * USD .005/GBP = **USD 400K**

Cap = 1.65USD/GBP * GBP 10M = USD 16.5M \Rightarrow Net cap = **USD 16.9M**

Note: The tradeoff is very clear: The higher the cost, the better the coverage.

2. (Closest At-the-money) In-the-money ($S_t \geq X$)

Call used: $X_c = 1.58$ USD/GBP, $p_c = \text{USD } .07$

Cost = Total premium = **USD 700K**

Cap = USD 15.8M \Rightarrow Net cap = **USD 16.5M**

Compare to Out-of-the-money: Advantage: Lower cap.

Disadvantage: Its cost.

Companies do not like to pay high premiums. Many firms finance the expense of an option by selling another option. A typical strategy: A collar (form a portfolio with one put and one call: Long one option, short the other).

3. Collar (buy one call, sell one put. In general, both are OTM)

Buy Call ($X_c = 1.63$ USD/GBP, $p_c = \text{USD } .05$);

Sell Put ($X_p = 1.58$ USD/GBP, $p_p = \text{USD } .055$)

Collar's premium = $\text{USD } .05 - \text{USD } .055 = \text{USD } -0.005$ (negative!)

Cost = $\text{GBP } 10\text{M} * \text{USD } (-.005/\text{GBP}) = \text{USD } -50\text{K}$

Cap = $1.63 \text{ USD/GBP} * \text{GBP } 10\text{M} = \text{USD } 16.3\text{M}$

Floor = Best case scenario = $1.58 \text{ USD/GBP} * \text{GBP } 10\text{M} = \text{USD } 15.8\text{M}$

\Rightarrow Net cap = **USD 16.25**; Net floor = **USD 15.75M**

Notes:

◊ With a collar you get a lower cost (advantage), but you give up the upside of the option (disadvantage) \Rightarrow there is always a trade-off!

◊ Zero cost insurance is possible \Rightarrow sell enough options to cover the premium of the option you are buying.

CHAPTER 11 - BONUS COVERAGE: Getting probabilities from the Empirical Distribution

Firms will use probability distributions to make hedging decisions. These probability distributions can be obtained using the empirical distribution, a simulation, or by assuming a given distribution. For example, a firm can assume that changes in exchange rates follow a normal distribution. Here, we present an example on how to use the empirical distribution.

Example: We want to get probabilities associated with different exchange rates. Let's take the historical monthly USD/AUD exchange rates 1976:1-2017:1. First, we transform the data to changes ($e_{f,t}$). Excel produces a histogram, with bins and frequency. Below we show the bins for $e_{f,t}$ frequency and relative frequency. We calculate $S_{t+30} = S_t * (1+e_{f,t})$. Today, $S_t = 0.7992$ USD/AUD.

$e_{f,t}$ (USD/AUD)	Frequency	Rel frequency	$S_t = .7992 * (1+e_{f,t})$
-0.17761	1	0.002049	0.657257
-0.16533	1	0.002049	0.667066
-0.15306	0	0	0.676874
-0.14079	0	0	0.686682
-0.12852	0	0	0.69649
-0.11624	1	0.002049	0.706298
-0.10397	1	0.002049	0.716106
-0.0917	2	0.004098	0.725914
-0.07943	4	0.008197	0.735722
-0.06715	4	0.008197	0.745531
-0.05488	6	0.012295	0.755339
-0.04261	12	0.02459	0.765147
-0.03034	29	0.059426	0.774955
-0.01806	56	0.114754	0.784763
-0.00579	86	0.17623	0.794571
0.006481	91	0.186475	0.804379
0.018753	82	0.168033	0.814187
0.031025	54	0.110656	0.823996
0.043298	29	0.059426	0.833804
0.05557	18	0.036885	0.843612
0.067843	8	0.016393	0.85342
0.080115	3	0.006148	0.863228
More	5	0.010246	0.871128

You can plot the histogram to get the above empirical distributions.

